## **Binary Trees**

Lecture 30 Section 19.1

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Wed, Apr 5, 2017

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- Binary Tree Applications
  - Binary Search Tree
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## **Binary Trees**

#### **Definition (Binary Trees)**

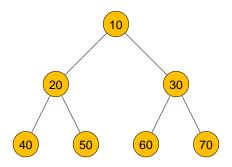
A binary tree is a data structure with the following properties.

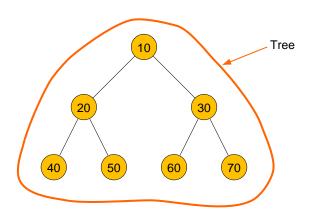
- It is either empty or it has a root node.
- Each node in the binary tree may be linked to up to two other nodes, called the left and right children.
- Each node, except the root node, has exactly one parent. The root node has no parent.

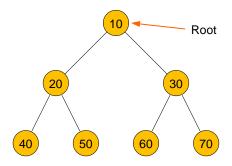
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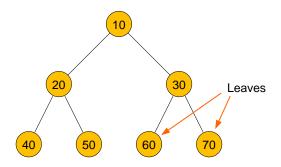
# **Binary Tree Terminology**

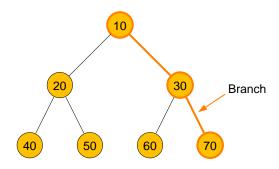
- The tree metaphor tree, root, branch, leaf.
- The family metaphor parent, child, sibling, ancestor, descendant.

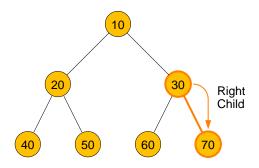


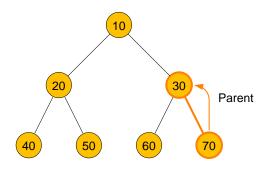


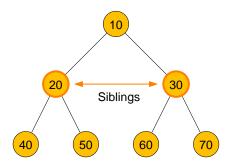












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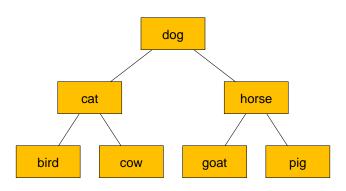
## **Binary Search Tree**

#### Definition (Binary search tree)

In a binary search tree, at every node,

- Every element in the left subtree is less than or equal to the element at the node.
- Every element in the right subtree is greater than or equal to the element at the node.
- Storing words in alphabetical order in a binary search tree allows for very rapid look-up.

## **Binary Search Tree**



{bird, cat, cow, dog, goat, horse, pig}

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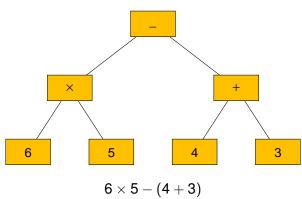
## **Binary Search Tree**

#### Definition (Binary search tree)

In a binary expression tree, at every interior node,

- The node element is an operator.
- The left subtree represents the left operand of the operator at the node.
- The right subtree represents the right operand of the operator at the node.
- It is very easy to evaluate an expression in a binary expression tree.

## **Binary Search Tree**



$$6\times5-(4+3)$$

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## **Binary Tree Implementation**

#### Binary Tree Node Data Members

- T m\_value
- BinaryTreeNode<T>\* m\_left
- BinaryTreeNode<T>\* m\_right
- m value The value stored in the node.
- m\_left A pointer to the left child node or NULL.
- m\_right A pointer to the right child node or NULL.

## **Binary Tree Implementation**

#### Binary Tree Data Member

- BinaryTreeNode<T>\* m\_root
- m\_root A pointer to the root node or NULL.

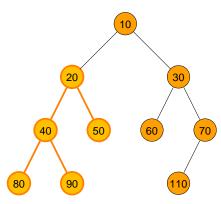
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#### Insertions and Deletions

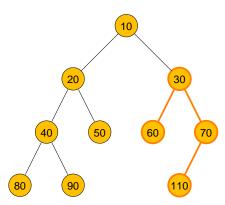
- Insertions and deletions in a binary tree are considerably more complicated than they were for linked lists.
- That is because a binary tree is not linear.
- Where should the new node be inserted?
- How would we specify a position?
- When a node is deleted, how is the hole filled?

- The size() function returns the number of nodes in the tree.
- Since the size of the tree is not stored as a data member, we will need to count the nodes.

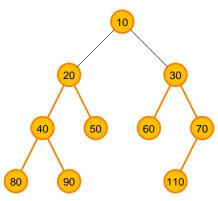
- How do we count the nodes in a binary tree?
- Think recursively.
- There is the root node.
- There are the nodes in the left subtree.
- There are the nodes in the right subtree.



Size of left subtree = 5



Size of right subtree = 4



Size of tree = 1 + 5 + 4 = 10

• Therefore,

$$size(root) = 1 + size(left) + size(right).$$

```
Example (Public, Nonrecursive size() Function)
int size() const
{
    return size(m_root);
}
```

#### Example (Private, Recursive size() Function)

```
int size(BinaryTreeNode* node) const
{
    if (node == NULL)
        return 0;
    else
        return 1 + size(node->m_left) + size(node->m_right);
}
```

## The search () Function

#### The search() Function

```
BinaryTreeNode* search(T value) const;
```

- The search() function has the above prototype
- It returns a pointer to the node where the value was found, or
- It returns NULL if the value was not found.

## The search() Function

• Write the public and private search () functions.

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# **Assignment**

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• Read Section 19.1.